

PyTorch Cheatsheet - Part 1

Useful activation function and torch.nn.functional

- Linear function: $y = WX + b$ where W and X are vectors of size N (number of dimensions to the input).

```
torch.nn.Linear(in_features, out_features, bias=True, device=None, dtype=None)
```

- Sigmoid function: $\frac{1}{1+e^{-z}}$ where z is the logit(s).

```
torch.nn.functional.sigmoid(input)
```

- Softmax function: $p(Y = t|x) = \frac{\exp(w_t^T x)}{\sum_{y \in \{0, \dots, C-1\}} \exp(w_y^T x)}$

```
torch.nn.functional.softmax(input, dim=None, _stacklevel=3, dtype=None) [source]
```

Loss Functions

- Mean squared error: $\ell(x, t; w) = (y - t)^2$

```
torch.nn.MSELoss(size_average=None, reduce=None, reduction='mean')
```

- Minimum log-likelihood: $\ell(x, t; w) = \sum_{(x^{(i)}, t^{(i)}) \in \mathcal{D}} -\log p(t|x)$

- Combined with binary classification: $\ell(x, t; w) = \sum_{(x^{(i)}, t^{(i)}) \in \mathcal{D}} \log(1 + \exp(-t^{(i)} w^T x^{(i)}))$

- Combined with softmax: $\ell(x, t; w) = \sum_{(x^{(i)}, t^{(i)}) \in \mathcal{D}} \left(-w_{t^{(i)}}^T x + \log \sum_{c \in \{0, \dots, C-1\}} \exp(w_c^T x) \right)$

```
torch.nn.CrossEntropyLoss(weight=None, size_average=None, ignore_index=-100, reduce=None, reduction='mean', label_smoothing=0.0) [source]
```

- Cross Entropy Loss:

- Linear (SVM formulation): $\ell(x, t; w) = \frac{|W[1:1]|}{2} + C \sum \max(0, 1 - t^{(i)} \cdot W x^{(i)})^2$

- Logistic: $\ell(x, t; w) = -t \log y - (1-t) \log(1-y)$

Optimizers and torch.optim

In standard gradient descent, the update rule is: $\mathbf{w}_{k+1} = \mathbf{w}_k - \alpha \nabla f(\mathbf{w}_k)$. In *gradient descent with momentum*, we introduce a *velocity term* v_k : $\mathbf{v}_{k+1} = \beta v_k - \alpha \nabla f(\mathbf{w}_k)$ and $\mathbf{w}_{k+1} = \mathbf{w}_k + v_{k+1}$ where: α is the learning rate, $\beta \in [0, 1]$ is the momentum coefficient, and v_k is the velocity term.

The following are some useful optimizers provided by the torch.optim library including:

- Stochastic gradient descent

```
torch.optim.SGD(params, lr=0.001, momentum=0, dampening=0, weight_decay=0, nesterov=False, *, maximize=False, foreach=None, differentiable=False, fused=None) [source]
```

PyTorch datasets

Required functions for dataset class:

- `__init__`: The `__init__` method is the constructor for the new dataset.
- `__len__`: The `__len__` method overrides the `len()` function in Python to determine the length of the dataset.
- `__getitem__`: The `__getitem__` method overloads the use of brackets to index items in a dataset.

There are lots of cool dataloader attributes and methods including:

- `batch_size`: number of examples in each batch or call to the dataloader
- `shuffle`: Boolean option to shuffle dataset each pass or *epoch* through the dataset
- `sampler`: *Sampler* object that specifies how data will be extracted from the dataset. For example, the *SubsetRandomSampler* allows us to specify indices within the larger dataset to sample at random.

Other useful equations

- Gradient descent: $\mathbf{w} \leftarrow \mathbf{w} - \alpha \frac{\partial \mathcal{E}}{\partial \mathbf{w}}$
- Closed form solution for linear regression: $W = (X^T X)^{-1} X^T T$
- L2 Regularization with MSE: $L(w) = \|y - Xw\|^2 + \lambda \|w\|_2^2$, closed form linear regression solutions: $W = (X^T X + \lambda I_d)^{-1} X^T y$
- Support Vector Machines - Margins at $WX = 1$ and $WX = -1$, border at $WX = 0$. Margin width = $2/\|W\|$

Sample Code

Here is a sample, two-dimensional logistic classifier code:

```
import numpy as np
import matplotlib.pyplot as plt
import torch
import torch.nn as nn
from torch.utils.data import Dataset
from torch.utils.data import DataLoader
from torch.utils.data import SubsetRandomSampler

class LogisticRegression(nn.Module):
    def __init__(self, N):
        super().__init__()
        self.w = nn.Parameter(torch.ones(N))
        self.b = nn.Parameter(torch.zeros(1))

    def forward(self, x):
        return 1/(1+torch.exp(-(self.w@x+self.b)))

class TwoClassDataset(Dataset):
    # don't forget the self identifier!
    def __init__(self, N, sigma):
        self.N = N # number of data points per class
        self.sigma = sigma # standard deviation of each class cluster
        self.plus_class = self.sigma*torch.randn(N, 2) + torch.tensor([-1, 1])
        self.negative_class = self.sigma*torch.randn(N, 2) + torch.tensor([1, -1])
        self.data = torch.cat((self.plus_class, self.negative_class), dim=0)
        self.labels = torch.cat((torch.ones(self.N), torch.zeros(self.N)))

    def __len__(self):
        return len(self.labels)

    def __getitem__(self, idx):
        x = self.data[idx]
        y = self.labels[idx]
        return x, y # return input and output pair

N = 100
sigma = 1.5
dataset = TwoClassDataset(N, sigma)
plus_data = dataset.plus_class
negative_data = dataset.negative_class

# create indices for each split of dataset
N_train = 60
N_val = 20
N_test = 20
indices = np.arange(len(dataset))
np.random.shuffle(indices)
train_indices = indices[:N_train]
val_indices = indices[N_train:N_train+N_val]
test_indices = indices[N_train+N_val:]

# create dataloader for each split
batch_size = 8
train_loader = DataLoader(dataset, batch_size=batch_size, sampler=SubsetRandomSampler(train_indices))
val_loader = DataLoader(dataset, batch_size=batch_size, sampler=SubsetRandomSampler(val_indices))
test_loader = DataLoader(dataset, batch_size=batch_size, sampler=SubsetRandomSampler(test_indices))

criterion = nn.BCELoss(reduction='mean') # binary cross-entropy loss, use mean loss
logreg_model = LogisticRegression(2) # initialize model
optimizer = torch.optim.SGD(logreg_model.parameters()) # initialize optimizer

n_epoch = 200 # number of passes through the training dataset
loss_values, train_accuracies, val_accuracies = [], [], []
for n in range(n_epoch):
    epoch_loss, epoch_acc = 0, 0
    for x_batch, y_batch in train_loader:
        optimizer.zero_grad()
        predictions = logreg_model(x_batch.unsqueeze(-1)).squeeze(-1)
        loss = criterion(predictions, y_batch)
        loss.backward()
        optimizer.step()

        epoch_loss += loss.item()
        epoch_acc += (predictions > 0.5).sum().item() / len(x_batch)

    loss_values.append(epoch_loss / len(train_loader))
    train_accuracies.append(epoch_acc / len(train_loader))

    if n % 10 == 0:
        print(f'Epoch {n}: Loss = {epoch_loss}, Accuracy = {epoch_acc / len(train_loader)}')

    if n == n_epoch - 1:
        print(f'Training complete! Final Loss = {epoch_loss}, Accuracy = {epoch_acc / len(train_loader)}')
```